

~ Dec 2007 : LHC starts

PP : $E_{cm} \sim 1 \text{ TeV} \rightarrow 14 \text{ TeV } 2008$

- EW symmetry breaking
- Next layers of structure

Compositeness?
SUSY?
Grand unif?
Extra dims?
Strings/DHs?
other?

This course:

- Overview current knowledge
- Importance of TeV scale
- Summarize some scenarios beyond.

... Primer - what LHC could begin to reveal.

→ logistics

Theoretical framework:

Effective field theory

review:

Practical necessity (§§): organize knowledge by energy.

Basic tenets for low energy physics ($E \ll M_p \sim 10^{19} \text{ GeV} ?$)

1. Lorentz invc (SRT)
2. Quantum mechanical
Hilb. space, superposition, hamiltonian, ...
3. Local

Folk theorem (221; QFT texts):

1+2+3 \Rightarrow QFT

n.b. include gravity \Rightarrow problems @ $E \sim M_p$

likely 1, 2, or 3 fail.

guess: locality

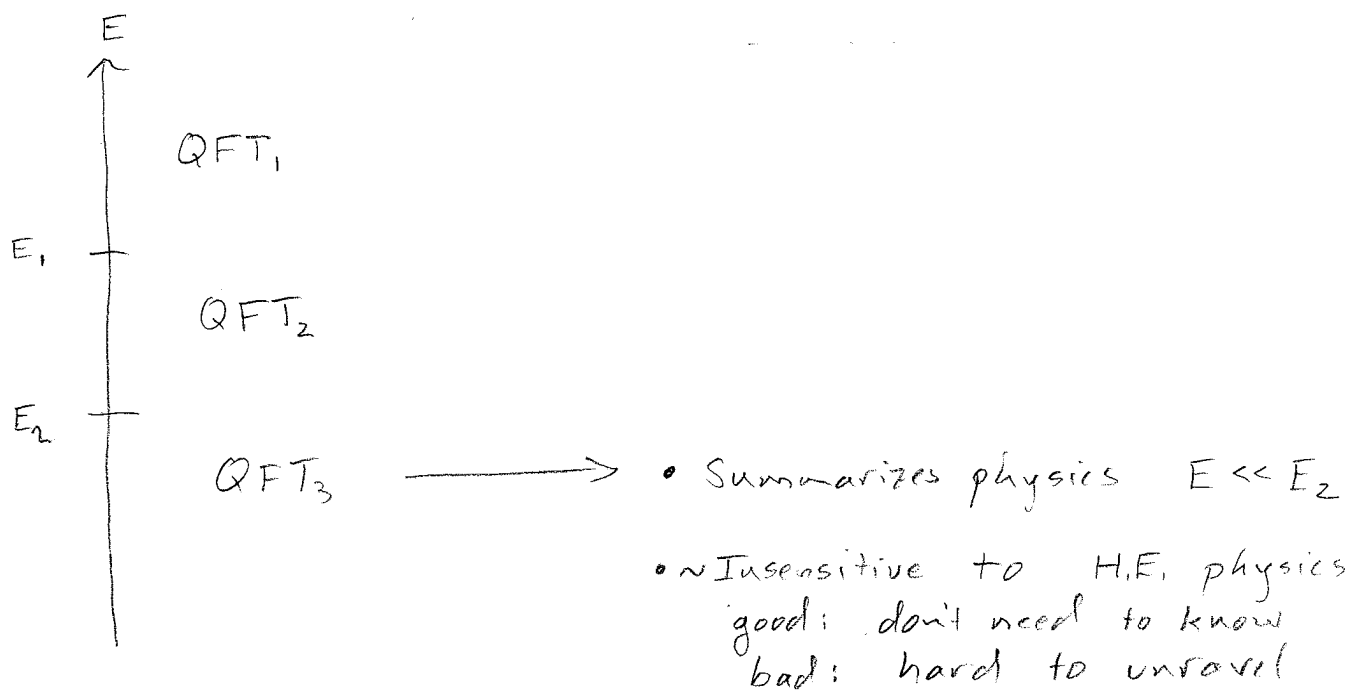
e.g. strings $\bullet \rightarrow \text{blob}$

or: grav. effects \Rightarrow more radical nonlocality?

LHC likely won't probe ... but in theories w/ TeV gravity
(large/warped extra dims) could ...

So: assume QFT (for now)

Hierarchies of QFTs



\leadsto QFT₃ is Low-energy effective theory of QFT_{2,1}

... a major theme of this course. (Read: Rotstein, p 1-22)

Critical organizing principle: Symmetry

(EFTs largely characterized by.)

1. \Rightarrow Poincare invariance:

Lorentz + translations
 $SO(3,1)$

Wigner: in QM a sym. must be represented by a unitary or antiunitary operator.

Lorentz reps: $SO(3,1) \sim SO(4) \approx SU(2) \times SU(2)$
 cf. eg. Srednicki

see from $[M_{\mu\nu}, M_{\rho\sigma}] = i\eta_{\mu\rho} M_{\nu\sigma} \pm \text{perms.}$

↑ know reps

Examples:

Rep	Name	spin	notation
$(1,1)$	scalar	0	$\phi(x), \dots$
$(2,1)$	LH spinor	$1/2$	$\psi_{\alpha}(x), \dots$
$(1,2)$	RH spinor	$1/2$	$\chi^{\dot{\alpha}}(x), \dots$
$(2,2)$	Vector	$0, 1$	$V^{\mu}(x), \dots$
$(3,2)$	LH spin $3/2$	$3/2, 1/2$	$\psi_{\alpha}^{\mu}(x)$
$(2,3)$	RH spin $3/2$	$3/2, 1/2$	$\psi^{\mu\dot{\alpha}}(x)$
$(3,3)$	rank 2 tensor	$2, 1, 0$	$h_{\mu\nu}(x)$
\vdots			

Conventions: largely \sim Srednicki (good practice - reconcile)

Particles = irreps of Poincare $M_{\mu\nu}, P_\lambda$

$$[M_{\mu\nu}, P_\lambda] = i\eta_{\mu\lambda}P_\nu - i\eta_{\nu\lambda}P_\mu$$

\leadsto extra conditions.

characterize by Casimirs:

$$P^2 \quad \checkmark$$

$$W^M = \frac{1}{2} \epsilon^{\mu\nu\lambda\sigma} P_\nu M_{\lambda\sigma} \quad \dots \text{Pauli-Lubanski} \sim \text{spin}$$

$\leadsto W^2$ (ex.)

Reps: (cf eg. Ramond)

$$1) \quad P^2 = -m^2 \quad \Rightarrow \quad W^2 = m^2 s(s+1) \quad s = 0, \frac{1}{2}, 1, \dots$$

$$\text{states: } |m, s, \vec{P}, s^z\rangle$$

$$2s+1$$

eg. $s = \frac{1}{2}$: Dirac ferm.

$$2) \quad P^2 = 0, \quad W^2 = 0; \quad W_\mu P^\mu = 0 \Rightarrow W_\mu \propto P_\mu$$

$$\text{indeed } W_\mu = \pm s P_\mu \quad s = 0, \frac{1}{2}, 1, \dots$$

$$|0, s, \vec{P}, \pm\rangle$$

2 \leftarrow eg vector w/constraints

$$3) \quad P^2 = 0, \quad W^2 > 0 \quad \text{spin continuous}$$

unphysical

$$4) \quad P^2 = m^2 > 0 : \quad \text{tachyon}$$

unphysical

... the possible particles

Dynamics: $\mathcal{L}(\phi^A, \partial_\mu \phi^A, \dots)$... Lorentz scalar.
 (eg.'s to come ...)
 ↑
 fields

Other symmetries

Discrete P, T, C
 ↑
 not spacetime: internal

Internal symmetries:

group $G \ni g$: n -dim rep.

$$\phi \rightarrow U(g) \phi$$

↑ ↑
 n vector $n \times n$ rep. matrix

important implication:

Noether's theorem:

Suppose \mathcal{L} invt under continuous, global symmetry;
 ↑
 x -indep

then EOM \Rightarrow conserved current

$$\partial_\mu j^\mu = 0.$$

Conserved charge: $Q = \int d^3x j^0$

... generates the symmetry.

Global symm: $\phi \rightarrow U(g)\phi$

everywhere in
Universe

weird?

Gauge symmetry $\phi \rightarrow U(g(x))\phi$

↑
local

⇒ gauge bosons (shortly)

Another critical principle:

Scaling & relevance

Another transformation:

$$x^\mu \rightarrow s x^\mu$$

$$p_\mu \rightarrow s^{-1} p_\mu$$

$$\phi^A(x) \rightarrow s^{-d} \phi^A(sx)$$

d = canonical dimension,

- generically not a sym.
- sometimes classical symm
- generically g . effects spoil - anomaly
- preserved: : conformal field theories,
- special -

$$\text{E.g. } S = - \int d^4x \left[(\partial_\mu \phi)^2 + m^2 \phi^2 + \sum_n \lambda_n \mathcal{O}_n \right]$$

$$\begin{array}{ccc} \uparrow & & \nwarrow \\ \text{dim } 4 & & \text{dim } 2 \\ \leftrightarrow [\phi] = 1 & & \\ \uparrow \text{dim of} & & \end{array}$$

$s \rightarrow \infty$ (IR) : $m^2 \phi^2$ dominates

more general ($D=4$):

$[\mathcal{O}] < 4$ Relevant

$[\mathcal{O}] = 4$ Marginal

$[\mathcal{O}] > 4$ Irrelevant

$$\text{E.g. } \lambda_1 \mathcal{O}_1 = \frac{\phi^2 (\partial_\mu \phi)^2}{M^2} : [\mathcal{O}_1] = 6$$

← dim analysis

small effect as $s \rightarrow \infty$

\sim invisible unless \rightsquigarrow qualitatively new physics

Conversely : $s \rightarrow 0$ (UV) :

$[\mathcal{O}] < 4 \rightarrow$ "small"

$[\mathcal{O}] > 4 \rightarrow$ "large"

$\sim \mathcal{O}(1)$ effects when $p \sim M$.

Moreover: $[\mathcal{O}] > 4 \leftrightarrow$ non-renormalizable

Renorm gp: mixes w/ higher dim ops (∞ #)
 so for $p \sim M$, EFT fails: ~~predictivity~~
 replace w/ new EFT

Other RG features

- dims shifted: anomalous dims
- Let cutoff scale $\sim \Lambda$ (typically take $\Lambda \sim M$)

consider $\lambda_n \mathcal{O}_n$ w/ $[\mathcal{O}_n] = d_n < 4$

generically: $\delta \lambda_n \sim \Lambda^{4-d_n}$

e.g. scalar: $\delta m^2 \propto \Lambda^2$

so $m^2 \ll \Lambda^2 \Rightarrow$ fine tuning

exception: symmetry prevents.

typically happens if $\lambda_n \rightarrow 0$ restores symmetry
 (non-anomalous)

then $\lambda_n \ll \Lambda^{4-d_n}$

"technically natural"