

$$\Sigma_0 = \begin{pmatrix} & & I_2 \\ & 1 & \\ I_2 & & \end{pmatrix} \quad \text{breaks } SU(5) \rightarrow SO(5) \text{ (ex)}$$

Goldstones: $\dim SU(5) = n^2 - 1 = 24$
 $\dim SO(5) = \frac{n(n-1)}{2} = 10$
14

$$\Sigma(x) = e^{2i\pi/f \sum_0} \quad \uparrow \quad \pi^a x^a \quad a=1, \dots, 14$$

Now, gauge $[SU(2) \times U(1)]^2 < SU(5)$

$$T_1^a = \begin{pmatrix} \sigma^a/2 \\ \\ \end{pmatrix} \quad Y = \text{diag}(-3, -3, 2, 2, 2) \quad g_{1(1)} \quad g_{2(1)}$$

$$T_2^a = \begin{pmatrix} \\ -\sigma^a/2 \\ \end{pmatrix} \quad Y = \text{diag}(-2, -2, -2, 3, 3) \quad g_{1(2)} \quad g_{2(2)}$$

Σ_0 breaks this $\rightarrow SU(2) \times U(1)$ (ex.)

indeed, $\Pi = \begin{pmatrix} & \phi/\sqrt{2} & \tau^+ \\ \phi^+/\sqrt{2} & & \phi^0/\sqrt{2} \\ \tau & \phi^0/\sqrt{2} & \end{pmatrix} \quad + \text{ eaten}$
 \uparrow triplet of $SU(2)$.

Now: $g_{i(1)} = 0 \Rightarrow SU(3)_1$ global sym $\left(\begin{array}{c|c} 3 \times 3 & \\ \hline & \end{array} \right)$

$g_{i(2)} = 0 \Rightarrow SU(3)_2$ global sym. $\left(\begin{array}{c|c} & \\ \hline & 3 \times 3 \end{array} \right)$

Either prevents m_h ; acts as $\phi_i \rightarrow \phi_i + \epsilon_{i(1,2)}$ (ex)

\therefore if $g_{(1)}$ or $g_{(2)} = 0$, $m_h = 0$.

$\therefore \delta m_h^2 \propto g_{(1)} g_{(2)} \Lambda^2$

\uparrow two loop!

designer fine tuning ...

Such models can permit $\Lambda \sim 10 \text{ TeV}$,

avoiding little hierarchy problem

(more fundamentally, need \sim ETC, etc.)