

# Perturbation theory vs. nonlocality

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(hep-th/0606146;  
hep-th/0605196)

Plausible resolution of the info. paradox:  
nonlocality

How does Hawking's calculation miss the  
critical physics ?

Could be answered in two ways:

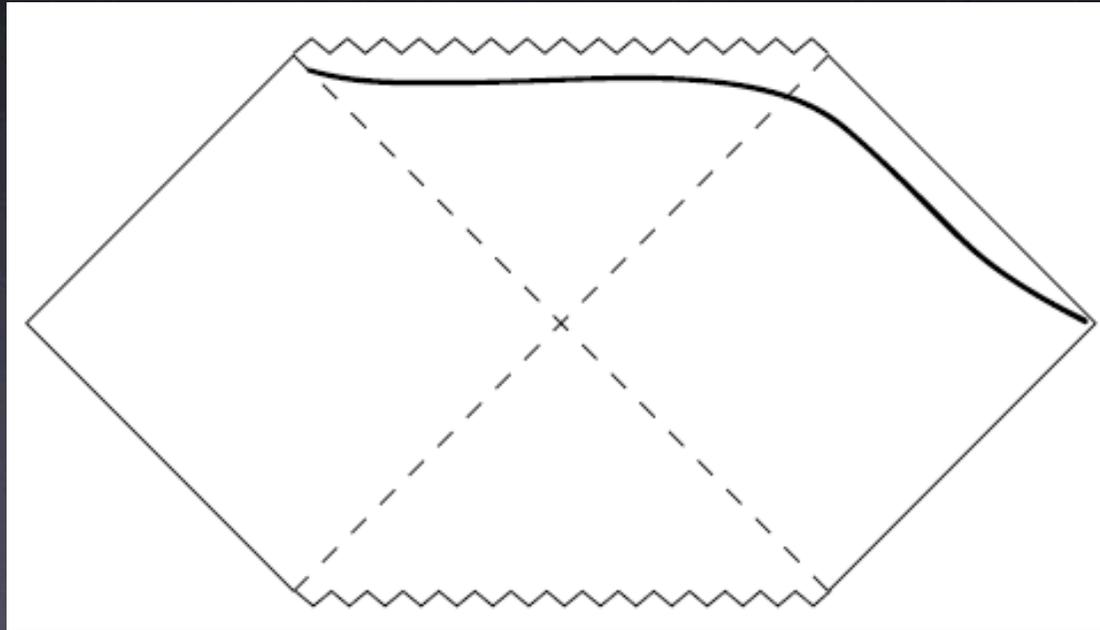
A. Compare *classical - quantum*, the H atom: classical physics doesn't break down at  $r_{atom}$ , it is *replaced*

B. Actual *breakdown* of semiclassical gravity

evidence for B...

Hawking's calculation (w/ updates):

$$\Delta I = S \leftarrow \rho \leftarrow |\psi\rangle \leftarrow |\psi\rangle_{NS}$$



Hawking's result: leading contribution -  
perturbative expansion in  $1/M_P$   
(fix  $M_P^{-2}M$ )

↔ QFT in semiclassical background (matter:  $\phi$ )

$$|\Psi\rangle \sim \int_{\Psi_{in}} \mathcal{D}h \mathcal{D}\phi e^{iS}$$

$$g_{\mu\nu} = g_{\mu\nu}^0 + M_P^{-1} h_{\mu\nu}$$

$$S \sim \int d^4x \sqrt{-g_0} \left\{ -(\nabla_0 \phi)^2 + h \Delta_L^0 h \right. \quad \text{semiclassical}$$

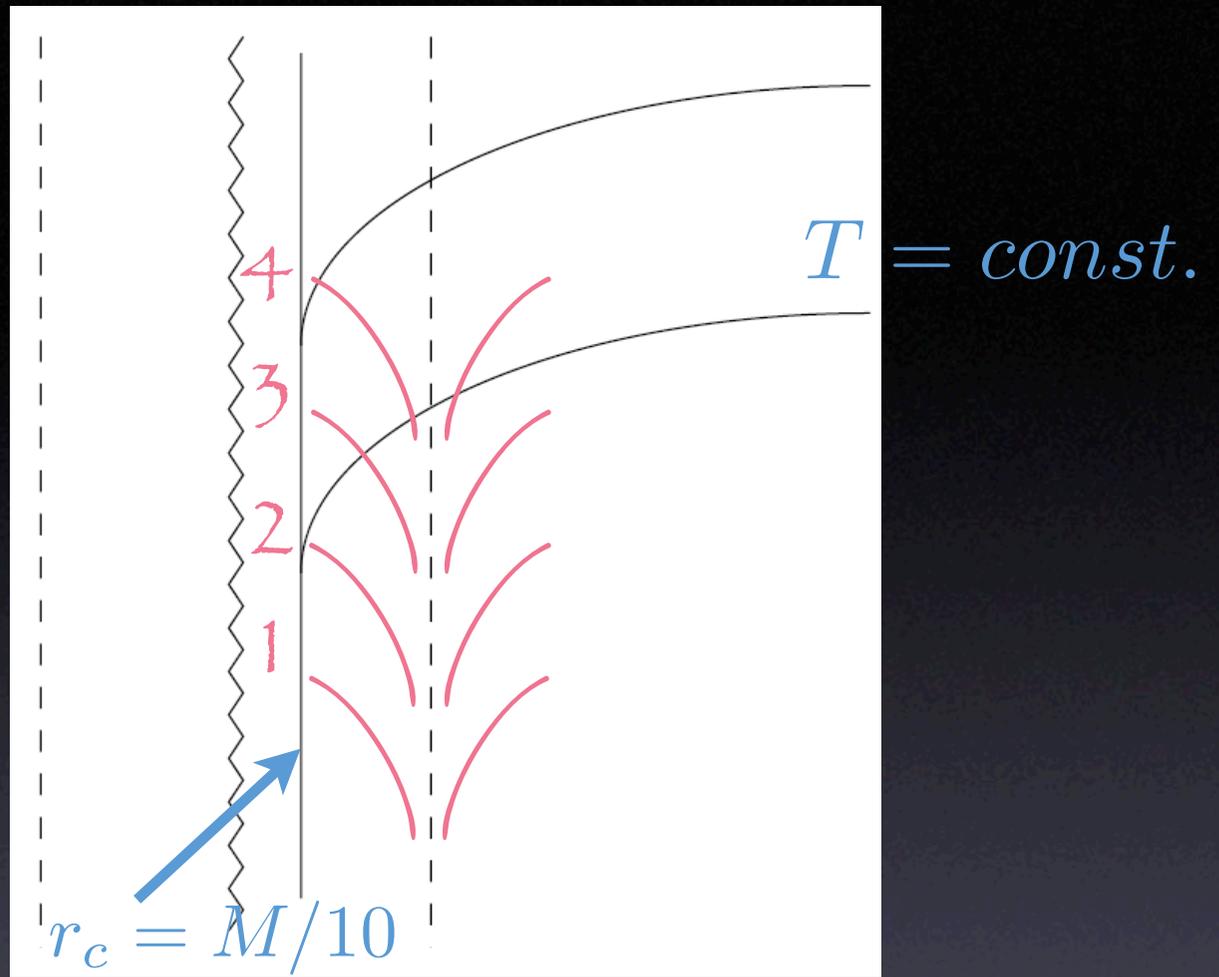
$$\left. + \frac{\hbar}{M_P} [T_{\mu\nu}^\phi + (\nabla h)^2] \dots \right\} \quad \frac{1}{M_P^n} \text{ terms}$$

$$= \sum_n M_p^{2-n} S_n$$

IMPORTANT?



Nice slices:

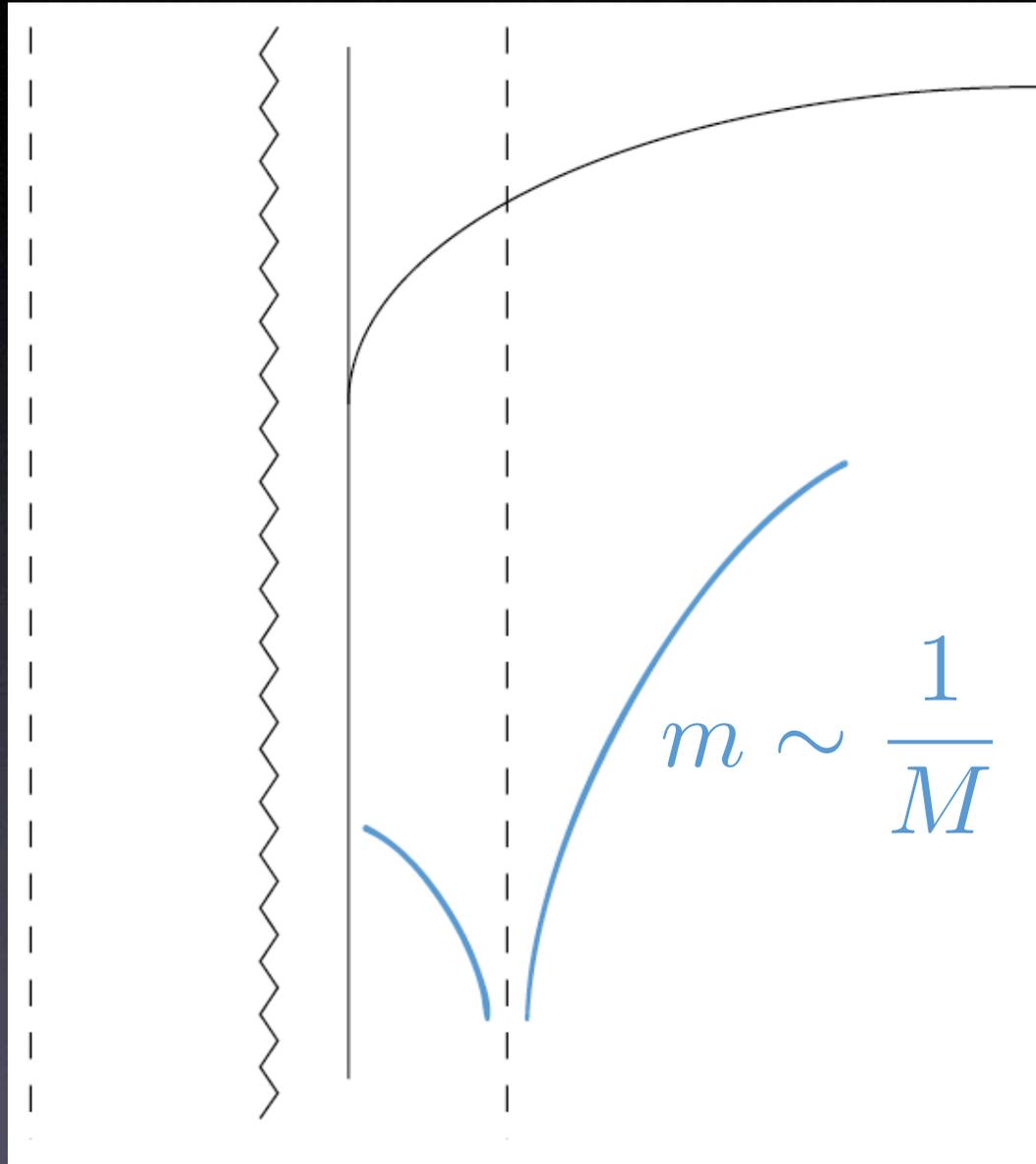


State:



$$\delta s \sim M \sqrt{\frac{2M}{r_c} - 1}$$

Consider a typical small fluctuation:



Extra quantum out,  
or throw one in

What is effect on state w/ or w/out  $M_P^{-1}$  terms?

Leading order:  $S = S_2$

QFT in background. No backreaction, no effect.

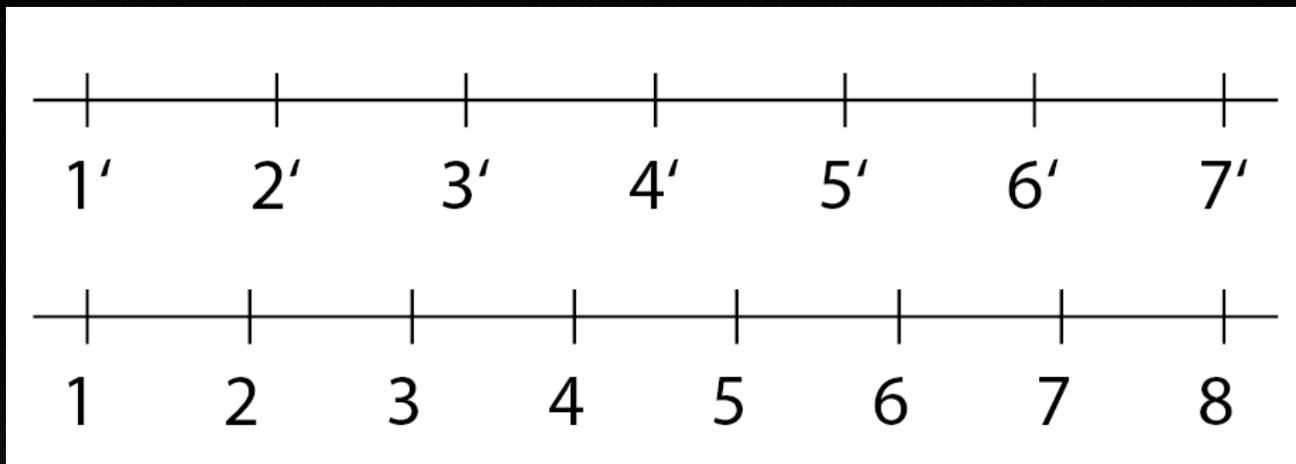
Perturbed:  $S = \sum_n M_p^{2-n} S_n$



$$\underbrace{\hspace{1.5cm}}_{\delta s'} \sim \delta s \left[ 1 + \mathcal{O}\left(\frac{m}{r_c}\right) \right]$$

$$\swarrow \mathcal{O}\left(\frac{1}{M^2}\right)$$

But:



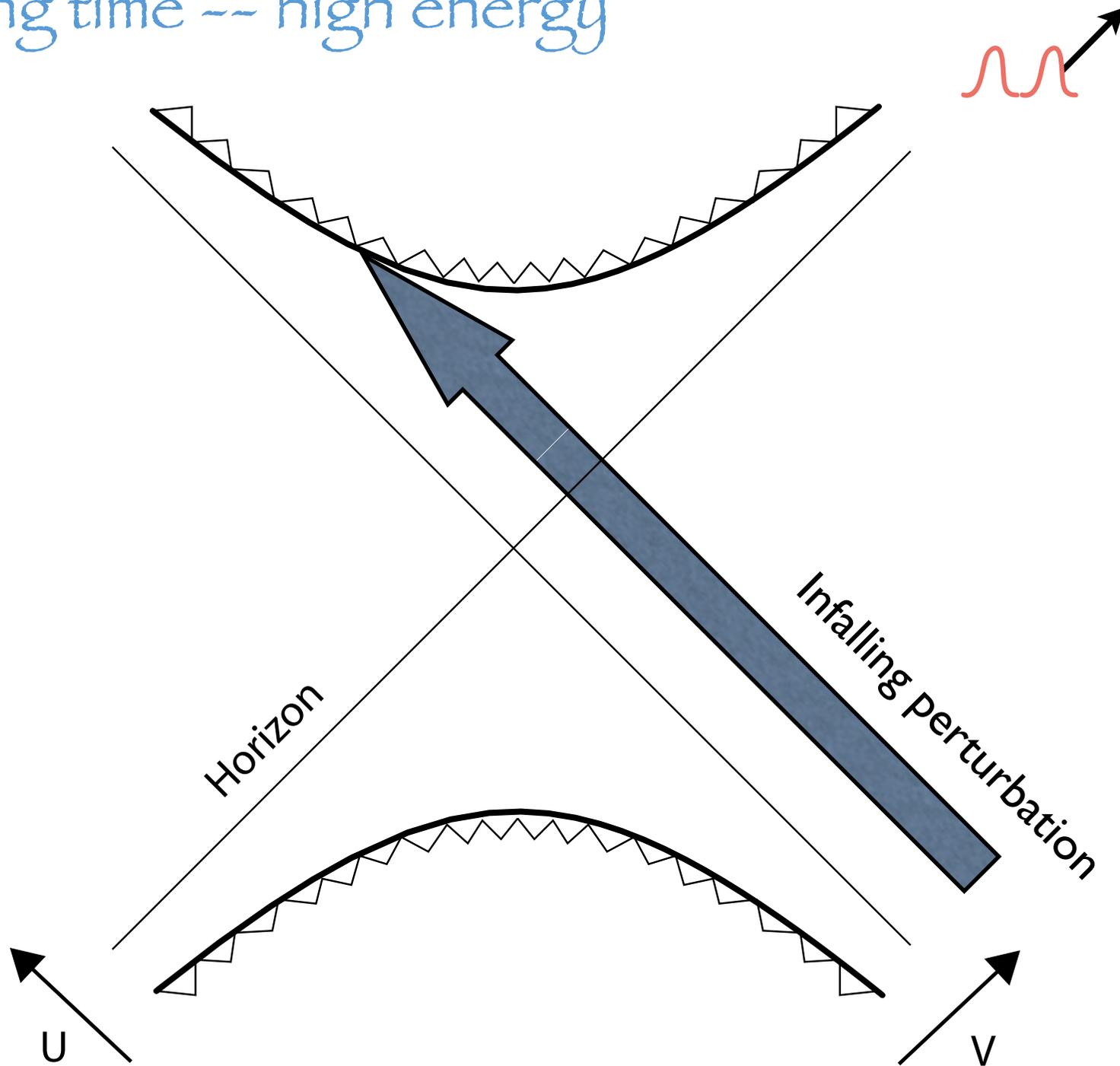
Long time: order one effect

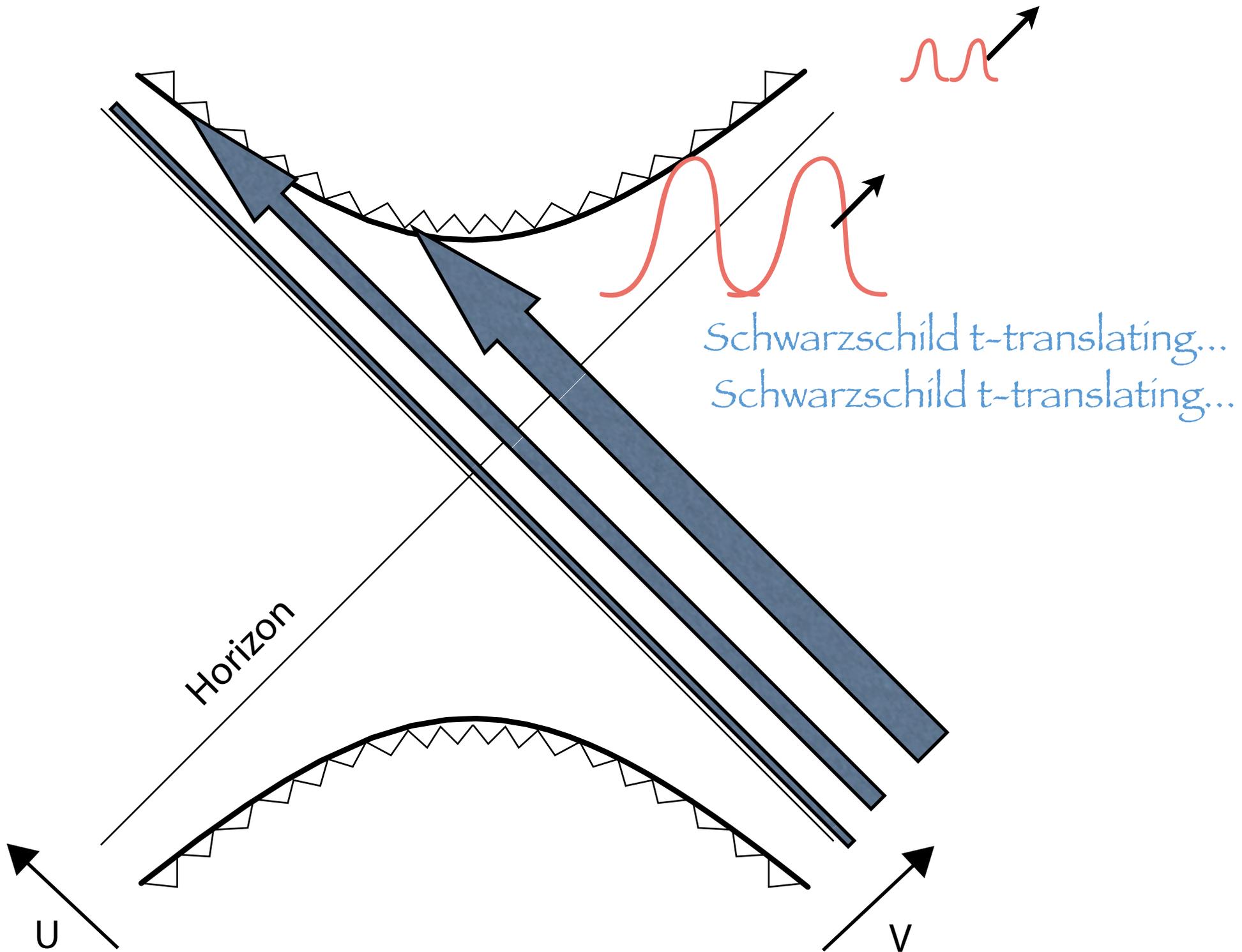
$$T \frac{m}{r_c} \sim M \quad \longleftrightarrow \quad T \sim M^3 \quad !$$

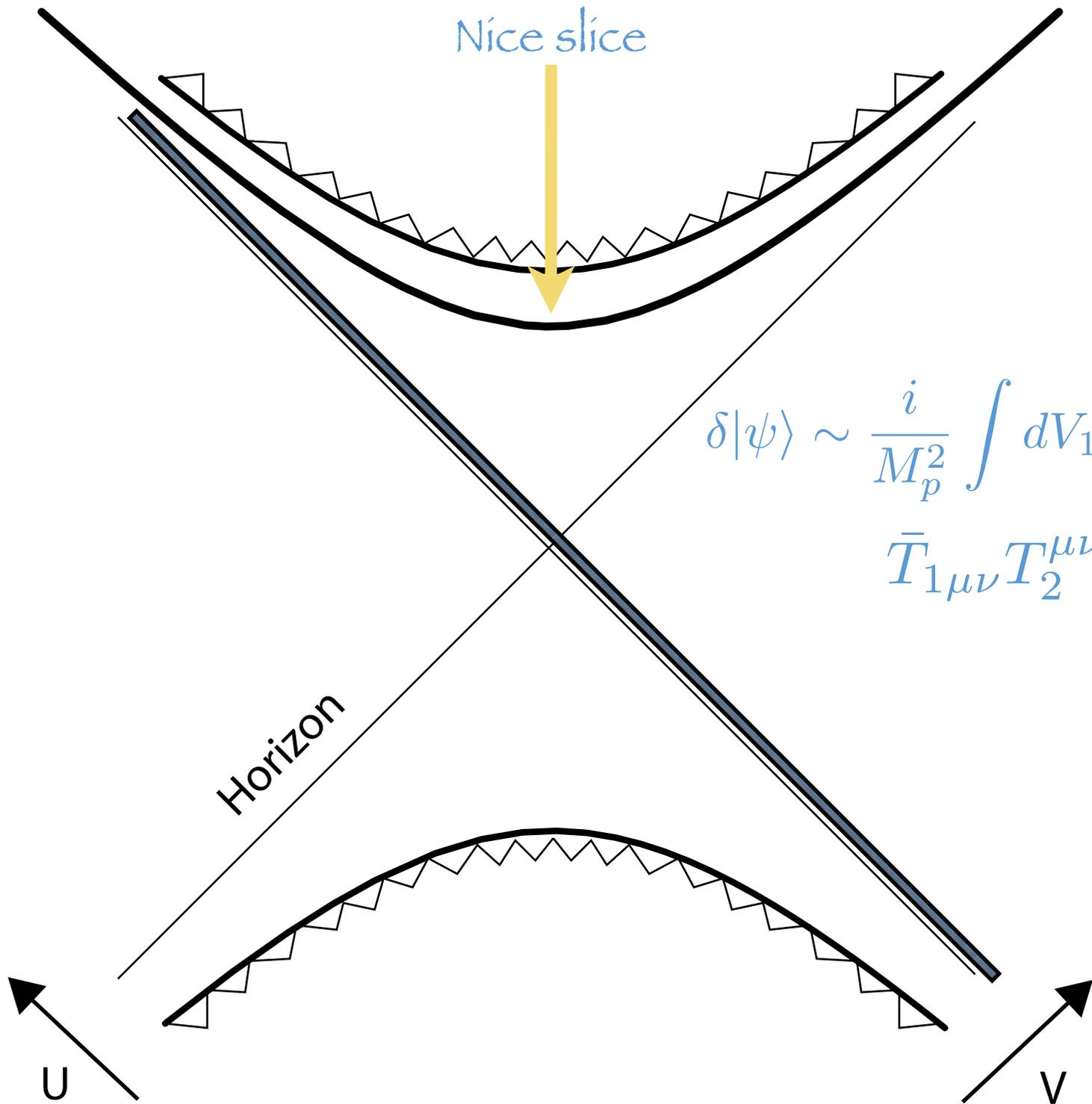
(cf. Page, 1993)

Large correlations between early perturbations/fluctuations and late state

Long time -- high energy







Nice slice

$$\delta|\psi\rangle \sim \frac{i}{M_p^2} \int dV_1 \int dV_2 \bar{T}_{1\mu\nu} T_2^{\mu\nu} G(x_1, x_2) |\psi_0\rangle$$

Horizon

u

v

Other large geom effects; gauge subtleties ...

Earlier estimate: deformation of geodesics

$$\Rightarrow T \sim M \ln M$$

Large effect on nice slice state

$$\Rightarrow T \sim M^3$$

True gauge invariant? (Bohr's dictum ...)

Drop in "depth charge" detectors  
(~relational obs.)

Large effect by  $T \sim M^3$

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- Can't trust this perturbative approach beyond this time (semiclassical approx)
- Such a calculation of the state apparently breaks down
- But this was our argument for information loss!
- If no reliable argument for info loss -- no paradox

general argument: locality?

Nonperturbative gravity:  
why should it be local?