RHK Ch. 18 Read K&K Ch. 5

Solve

From RHK Ch. 18 Exercises 11, 12, 20, 28. Problems 8, 10

From K&K Ch. 3 Problem 3.7

Problem 1. The wave equation according to an observer S motionless with respect to a string is

$$\frac{\partial^2 y}{\partial x^2} - \frac{1}{c^2} \frac{\partial^2 y}{\partial t^2} = 0,$$

where c is a wave speed. Show that another observer S' is moving at constant velocity v along the x-axis relative to S, will write the wave equation

$$\left(1 - \frac{v^2}{c^2}\right) \frac{\partial^2 y}{\partial x'^2} - \frac{1}{c^2} \frac{\partial^2 y}{\partial t'^2} + \frac{2v}{c^2} \frac{\partial^2 y}{\partial x' \partial t'} = 0,$$

where x' and t' are defined by the so-called Galilean transformation: x' = x - vt, t' = t.

Extra Credit. Show that the action for a simple harmonic oscillator of mass m and angular frequency ω and such that at t=0 the position is x_0 , and at time T the position is x_T , is given by

$$S = \frac{m\omega}{2\sin\omega T} \left[\left(x_0^2 + x_T^2 \right) \cos\omega T - 2x_0 x_T \right].$$