

UNIVERSITY OF CALIFORNIA, SANTA BARBARA
Department of Physics
2014 Winter Quarter

GALAXIES AND COSMOLOGY

Professor Treu

HOMEWORK #1
EMPIRICAL EVIDENCE FOR THE BIG BANG

Problem 1: **Neutrino mass**

Ryden, Problem 2.4.

Problem 2: **Planck's Law**

Treat the Sun as a blackbody of absolute temperature 5800 K. Use Stefan's law to show that the total radiant energy emitted by the Sun per second is $3.95 \times 10^{26} \text{ J s}^{-1}$. Find the rate at which energy is reaching the top of the Earth's atmosphere. Your answer should have units of flux – $\text{J s}^{-1} \text{ m}^{-2}$. *Hints: Stefan-Boltzmann constant $\sigma = 5.67 \times 10^{-8} \text{ J s}^{-1} \text{ m}^{-2} \text{ K}^{-4}$. The radius of the Sun is $7.0 \times 10^8 \text{ m}$, and the Sun – Earth distance is $1.5 \times 10^{11} \text{ m}$.*

Problem 3: **Tired light Universe**

Ryden, Problem 2.5.

Problem 4: **When was He formed?**

Assuming that the size of a He nucleus is 2 Fermi (10^{-15} m), estimate the epoch of He formation in a Big Bang cosmology, expressed in redshift and temperature. *Hint: order of magnitude estimate is sufficient.*

Problem 5: **Hot Dark Matter**

Assuming dark matter is in the form of massive neutrinos (of approximately equal mass), that the total mass density of the universe is 1 in critical units, and there is no dark energy, compute the required neutrino masses in eV.