## **American Wire Gauge**

## Phys 13 / Phys CS 15 Professor Everett Lipman

In the United States, wire diameters are specified according to the American Wire Gauge (AWG). There are 40 different sizes, ranging from 36 (smallest) to 0000 (largest, also written "4/0"): 36, 35, 34, ..., 2, 1, 0, 00, 000, 0000.

The diameter  $D_{36}$  of 36 AWG wire is 0.005'' (= 0.127 mm). The ratio of each diameter to the previous one is  $92^{1/39} = 1.1229322$  (I am not joking—you can't make this stuff up). Therefore, the diameter of n AWG wire is

$$D_n = D_{36} \, 92^{\frac{36-n}{39}},$$

where n must be negative for sizes 00 and larger. For example,

$$D_{22} = D_{36} 92^{14/39} = (0.127 \text{ mm}) \times 5.06931731 = 0.6438 \text{ mm}.$$

Some common sizes:

AWG	Diameter
10	2.588  mm = 0.1019''
14	1.628  mm = 0.0641''
18	1.024  mm = 0.0403''
22	0.644  mm = 0.0253''
24	0.511  mm = 0.0201''

What is the resistance of a length L of n AWG copper wire? The resistivity of copper is  $\rho_{\rm Cu} = 1.678 \times 10^{-8} \ \Omega$ ·m at 20 °C.

$$R = \rho_{\rm Cu} L / A$$

where A is the cross-sectional area of the wire. So

$$R = \frac{4\rho_{\rm Cu}L}{\pi D_n^2} = \frac{4\rho_{\rm Cu}L}{\pi D_{36}^2 92^{\frac{2\times(36-n)}{39}}}.$$

Working in SI units,  $D_{36} = 1.27 \times 10^{-4}$  m, so

$$\frac{4\rho_{\rm Cu}}{\pi D_{36}^2} = 1.3246 \ \Omega/{\rm m}.$$

Then

$$R = \frac{1.3246L}{92^{\frac{72-2n}{39}}} = 1.3246 \cdot 92^{\frac{2n-72}{39}}L \ \Omega,$$

where L is in meters.

Example: for n = 22 and L = 0.3 m,  $R = 1.55 \times 10^{-2} \Omega$ .